Deepening All Students' Understanding with Algebra Experiments



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Knot Tying Exploration

What happens to the length of a rope when one or more knots are tied into it? Follow the directions below to explore this question.

Materials:

Two pieces of rope with different diameters about 60 inches long, tape measure or yardstick

Directions:

- 1. Measure the length of the rope with no knots. Record it in the table.
- 2. Tie a knot in the rope, measure the length, and record it in the table.
- 3. Tie a second knot in the rope, measure the length, and record it in the table.
- 4. Continue tying knots in the rope, measure the length after each new knot, and record the data in the table.

Number of Knots	Length of Rope (inches)

- 6. Make a graph of your data using the number of knots as the independent variable and the length of the rope as the dependent variable.
- 7. Find the equation for the line of best fit.
- 8. Predict the length of the rope if 13 knots were tied.
- 9. Predict the length of the rope if 15 knots were tied.
- 10. Predict the number of knots if the length of the rope is 8 inches.
- 11. Predict the number of knots if the length of the rope is 13 inches.
- 12. What does the y-intercept represent in this situation?
- 13. What does the slope represent in this situation?
- 14. Are there any parts of the graph that have no real-world meaning in this situation? Explain why.
- 15. Repeat steps 1 7 with another rope with a different diameter.

 Compare your results. Make a conjecture about how different widths of rope affect the representations. Make a conjecture about how different lengths of the rope affect the representations.

Activity adapted from Key Curriculum Press's Discovering Algebra

Cereal Investigation



What is the relationship between the diameter of a lid and the amount of cereal needed to cover the inside of the lid? Investigation this question by following the directions below.

Materials: 6 lids of different sizes, cereal, ruler

Directions:

- 1. Select a lid. Measure its diameter in centimeters. Make sure the ruler goes through the center of the lid when measuring.
- 2. Fill the inside of the lid with a layer of cereal pieces. Count the number of pieces needed.
- 3. Record this information in the table.

Diameter of Lid (cm)	Number of Pieces of Cereal Needed to Cover the Lid

4. Repeat the steps 1-3 for 5 additional lids.

- 5. Make a graph of your data. Does the graph appear to be more linear or quadratic? Explain.
- 6. Find the equation for the curve of best fit.
- 7. What does the y-intercept represent in this situation?
- 8. How many pieces of cereal would be needed to cover a lid that measures 20 cm in diameter?
- 9. How many pieces of cereal would be needed to cover a lid that measures 40 cm in diameter?
- 10. What happens to the amount of cereal needed when the diameter doubles?
- 11. If 250 pieces of cereal are needed to cover the inside of a lid, what is the diameter of the lid?
- 12. Are there any parts of the graph that don't make sense in this situation? Explain.
- 13. How might the results of this investigation change if a different type of cereal is used?

Basketball Experiment



What happens to a person's shooting success when that person moves away from the basket? Simulate this situation by following the directions below.

Materials:

Paper bag with flat bottom or bucket, 10 pieces of paper, yardstick

Directions:

- 1. Place basket (paper bag or bucket) on floor.
- 2. Make 10 pieces of paper into 10 paper balls.
- 3. Stand 1 yard away from the basket.
- 4. One by one toss the 10 balls into the basket. Record the number of balls that went into the basket.

Distance from Basket (yards)	Number of Baskets

5. Step back 1 yard and repeat step 4.

- 6. Continue stepping back, shooting, and collecting data stopping when no baskets are made.
- 7. Make a graph of your data. Does the graph appear to be more linear, quadratic, or exponential? Explain.
- 8. Find the equation for the curve of best fit. Explain why your choice of equation makes sense in this situation.
- 9. What does the y-intercept represent in this situation?
- 10. What do each of the numbers in your equation represent in this situation?
- 11. If you stood 5.5 yards away from the basket, approximately how many baskets would you make?
- 12. If you stood 12 yards away from the basket, approximately how many baskets would you make?
- 13. If you made 6 baskets, approximately how many yards away from the basket would you be standing?
- 14. Compare your equation to the equations of others in your group. How are the equations similar? How are the equations different? What do the equations reveal about a person's shooting skills?
- 15. Are there any parts of the graph that have no real-world meaning in this situation? Explain why.